

Doppler Shift Calculations

Name:

Date:

Given information:

Speed of light = $c = 3 \times 10^5$ km/s

NaD line 1 (λ_1) = 5889.96 Angstroms

NaD line 2 (λ_2) = 5895.93 Angstroms

$\Delta\lambda_{\text{Line 1-2}} = \lambda_2 - \lambda_1 = 5.97$ Angstroms (used for conversion)

In the Excel template, determine the line minimums for the two lines (i.e. Left and Right or TopLeft and BottomLeft, etc.) with the largest shift. Below we call the two lines P1 (stands for “position 1 (on the solar disk)”) and P2.

Measurements from Excel Template:

$\text{Pix}_{\text{NaD_Line1@P1}}$ = _____ (in pixels)

$\text{Pix}_{\text{NaD_Line1@P2}}$ = _____ (in pixels)

$\text{Pix}_{\text{NaD_Line2@P1}}$ = _____ (in pixels)

$\text{Pix}_{\text{NaD_Line2@P2}}$ = _____ (in pixels)

$\text{Pix}_{\text{WaterLine@P1}}$ = _____ (in pixels)

$\text{Pix}_{\text{WaterLine@P2}}$ = _____ (in pixels)

Calculations:

Conversion factor from pixel to wavelength

Calculate the pixel separation between NaD line 1 and NaD line 2 for each solar disk positions. These should be the same value.

Position 1: $\Delta\text{pixel}_{\text{Line 1-2}}$ = _____

Position 2: $\Delta\text{pixel}_{\text{Line 1-2}}$ = _____

$\Delta\lambda_{\text{conversion}} = \Delta\lambda_{\text{Line 1-2}} / \Delta\text{pixel}_{\text{Line 1-2}}$ = _____

Doppler Shift

Apparent pixel shift in sodium lines:

$$\Delta \text{Pix}_{\text{Line1, apparent}} = \text{Pix}_{\text{NaD_Line1@P1}} - \text{Pix}_{\text{NaD_Line1@P2}} = \underline{\hspace{2cm}} \text{ (in pixels)}$$

$$\Delta \text{Pix}_{\text{Line2, apparent}} = \text{Pix}_{\text{NaD_Line2@P1}} - \text{Pix}_{\text{NaD_Line2@P2}} = \underline{\hspace{2cm}} \text{ (in pixels)}$$

Correction factor determined from apparent water line offset:

$$\Delta \text{Pix}_{\text{correction}} = \text{Pix}_{\text{WaterLine@P1}} - \text{Pix}_{\text{WaterLine@P2}} = \underline{\hspace{2cm}} \text{ (in pixels)}$$

True pixel shift in sodium lines:

$$\Delta \text{Pix}_{\text{Line1, true}} = \Delta \text{Pix}_{\text{Line1, apparent}} - \Delta \text{Pix}_{\text{correction}} = \underline{\hspace{2cm}} \text{ (in pixels)}$$

$$\Delta \text{Pix}_{\text{Line2, true}} = \Delta \text{Pix}_{\text{Line2, apparent}} - \Delta \text{Pix}_{\text{correction}} = \underline{\hspace{2cm}} \text{ (in pixels)}$$

True wavelength shift in sodium lines:

$$\Delta \lambda_{\text{Line1}} = \Delta \text{Pix}_{\text{Line1, true}} \text{ (in pixels)} * \Delta \lambda_{\text{conversion}} = \underline{\hspace{2cm}} \text{ (in Angstroms)}$$

$$\Delta \lambda_{\text{Line2}} = \Delta \text{Pix}_{\text{Line2, true}} \text{ (in pixels)} * \Delta \lambda_{\text{conversion}} = \underline{\hspace{2cm}} \text{ (in Angstroms)}$$

Rotational Velocity

Solve for ΔV , which is the difference of velocities at positions 1 and 2, using $\Delta V/c = \Delta \lambda / \lambda_{\text{Line 1}}$. The solar rotational velocity itself would then be the absolute value of $(\Delta V/2)$. Fill in the table below with actual numbers:

<u>Na D Line number</u>	<u>$\Delta \lambda$ (in Angstroms)</u>	<u>ΔV (in km/s)</u>	<u>V_{rotation} (in km/s)</u>
1	$\Delta \lambda_{\text{Line1}}$		
2	$\Delta \lambda_{\text{Line2}}$		
<i>Average</i>	X	X	